Course No. - 2.5 : Operations Research
Time : 3 Hours
Note : Answer All questions.

PART - A (10x2=20 Marks)

1. Write short notes on the following:
(a) Nature and Scope of OR
(b) What is Goal Programming?
(c) Sensitivity analysis in LPP
(d) Degeneracy in TP
(e) What is unbalanced transportation problem?
(f) What is restricted assignment problem?
(g) Stack time, resource leveling and Dummy activity
(h) Critical path
(i) Describe the maximini principle of game theory
(j) What are the types of simulation Models?

PART - B ( $5 \times 12=60$ Marks)
Answer all the questions using the internal choice .
2.(a) Describe the origin and development of operation research. What were the controlling factors giving birth to operation research?

## OR

(b) Solve the following linear programming problem graphically

Minimsie $Z=-x_{1}+2 x_{2}$
Subject to constraint : $-\mathrm{x}_{1}+3 \mathrm{x}_{2} \leq 10$

$$
\begin{array}{r}
\mathrm{x}_{1}+\mathrm{x}_{2} \leq 6 \\
\mathrm{x}_{1}-\mathrm{x}_{2} \leq 2 \\
\text { and } \mathrm{x}_{1}, \mathrm{x}_{2} \geq 0
\end{array}
$$

3.(a) ABC metal company produces two items P1 and P2. It uses sheet metal, equipment and labour. Input output relationship resources available as follows.

| Input | Product requirement per unit |  | Availability |
| :---: | :---: | :---: | :---: |
|  | P1 | P2 |  |
| Sheet metal | $1 \mathrm{sq} . \mathrm{cm}$ | 1 sq. cm | $50 \mathrm{sq} . \mathrm{cm}$ |
| Labour | 1 man hour | 2 man hour | 80 man hours |
| Equipment | 3 hours | 2 hours | 140 hours |
| Profit (Rs) | 4 per unit | 3 per unit |  |

How many units of P 1 and P 2 should be manufacture to maximised the profit of the company?

OR
(b) Solve the following problem by simplex method:

Max $Z=4 x_{1}+3 x_{2}$
Subject to constraints: $2 x_{1}+x_{2} \leq 1200$

$$
\begin{gathered}
x_{1}+x_{2} \leq 700 \\
3 x_{1}+4 x_{2} \leq 2400 \\
\text { and } x_{1}, x_{2} \geq 0
\end{gathered}
$$

4.(a) Determine initial basic feasible solution to the following transportation problem using least cost method.

| Sources | Destinations |  |  |  | Supply |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ |  |
| $\mathrm{~S}_{1}$ | 21 | 16 | 15 | 3 | 11 |
| $\mathrm{~S}_{2}$ | 17 | 18 | 14 | 13 | 13 |
| $\mathrm{~S}_{3}$ | 32 | 27 | 18 | 41 | 19 |
| Demand | 6 | 10 | 12 | 15 |  |
| OR |  |  |  |  |  |

(b) A sales man has to visit 5 cities ABCD \& E. He wishes to start from a particular city, visit each city only once and then return to the starting city. The cost of traveling from, a city to another city is given. Determine the least cost route.
5.(a) Draw the net work diagram, identify critical path and compute the total, free and independent floats for the following data.

| Activity | Immediate predecessor activity | Duration |
| :---: | :---: | :---: |
| A | - | 8 |
| B | A | 9 |
| C | B | 7 |
| D | A | 15 |
| E | C,D | 4 |
| F | E | 1 |
| G | D | 4 |
| H | E,G | 5 |
| I | OR | 4 |

(b) Draw PERT network diagram for the data given below:

| Activity | Preceding Activity | Activity Time (weeks) |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{t}_{0}$ | $\mathrm{t}_{\mathrm{m}}$ | $\mathrm{t}_{\mathrm{p}}$ |
| A | -- | 4 | 7 | 13 |
| B | A | 6 | 9 | 11 |
| C | A | 5 | 7 | 9 |
| D | B | 3 | 5 | 7 |
| E | C | 7 | 8 | 10 |
| F | D | 2 | 3 | 5 |
| G | E | 6 | 7 | 8 |
| H | F,G | 2 | 3 | 4 |

(i) Find the expected duration of the project.
(ii) Compute the probability of completing the project in 35 weeks or less.
6.(a) In a bank, cheques are cashed at a single 'teller' counter, customers arrive at the counter in a Poisson manner at an average rate of 30 customers per hour. The teller takes on an average a minute and a half to cash the cheque. The service time has been found to be exponentially distributed.
(i) Calculate the percentage of time the teller is busy.
(ii) Calculate the average time a customer is expected to wait.

OR
(b) Solve the following game using dominance method and find value of the game.

> Player Q

$$
\text { Player } P \quad\left[\begin{array}{llll}
2 & 2 & 3 & 4 \\
4 & 3 & 2 & 2
\end{array}\right]
$$

